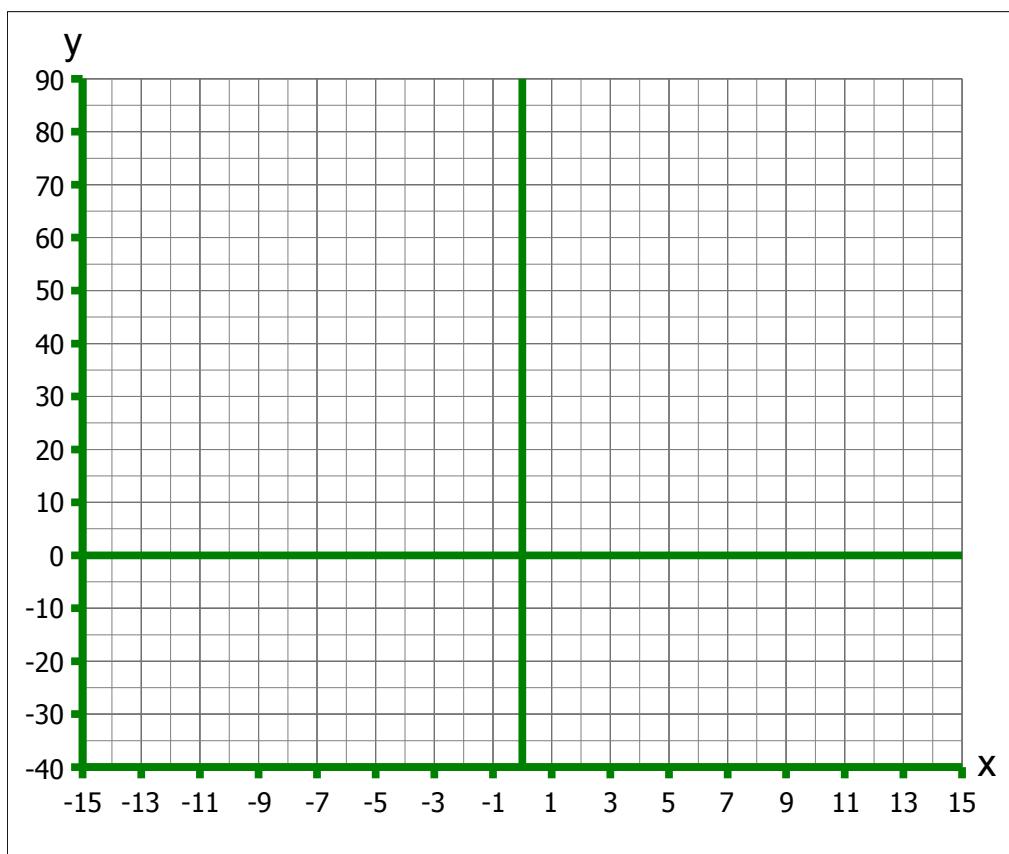


MS 100 College Algebra Midterm summer 2007 Name:

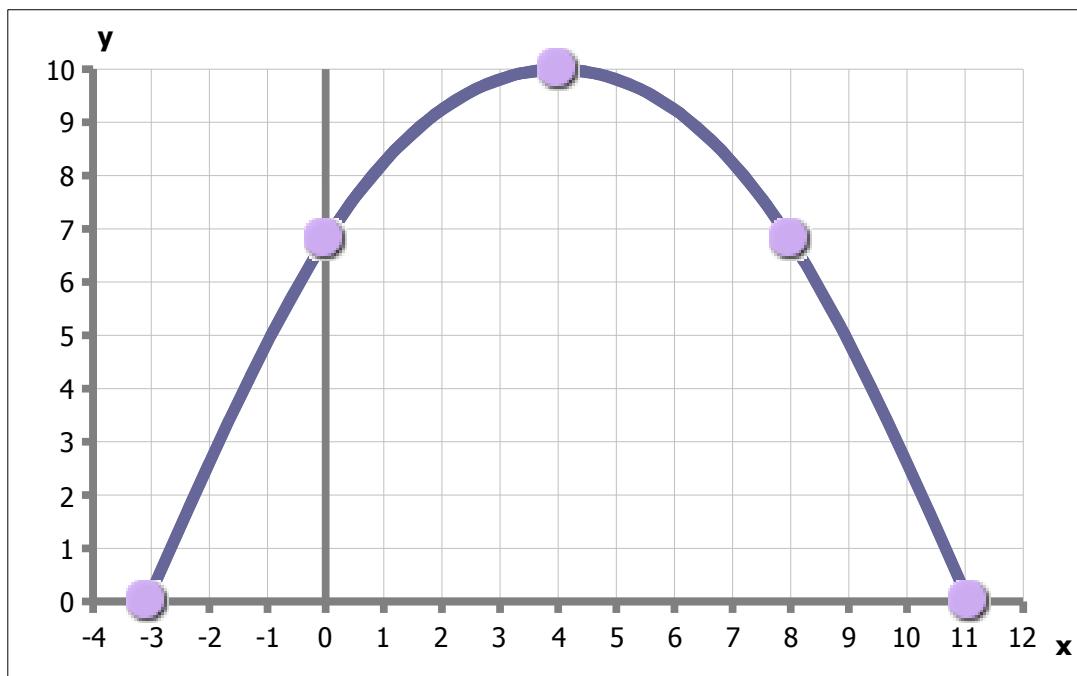
file and version info: fjord.odt 200707151632

1. Find the y-intercept for  $f(x) = -x^2 + 4x + 77$  (0, \_\_\_\_\_)
2. Find the zeros of the function  $f(x) = -x^2 + 4x + 77$  (\_\_\_\_\_, 0) (\_\_\_\_\_, 0)
3. Find the axis of symmetry for  $y = -x^2 + 4x + 77$  x = \_\_\_\_\_
4. Find the vertex (h, k) for  $y = -x^2 + 4x + 77$  (\_\_\_\_\_, \_\_\_\_\_)
5. Rewrite  $y = -x^2 + 4x + 77$  in vertex form:  $(y - _____) = _____ (x - _____)^2$
6. Given  $(y - k) = \frac{1}{4p}(x - h)^2$ , find the focus distance p for  $y = -x^2 + 4x + 77$ .  
 $p = _____$
7. Determine the coordinates of the focus for  $y = -x^2 + 4x + 77$ . (\_\_\_\_\_, \_\_\_\_\_)
8. Is the curvature of  $y = -x^2 + 4x + 77$  positive or negative? \_\_\_\_\_
9. Is  $f(x) = -x^2 + 4x + 77$  a function? \_\_\_\_\_
10. Is there an **inverse** function  $f^{-1}(x)$  for  $f(x) = -x^2 + 4x + 77$ ? \_\_\_\_\_
11. Sketch a graph of  $y = -x^2 + 4x + 77$  on the chart below.



The problems on this page deal with the following data:

Label	x	y	Coordinates
vertex	4	10	(4, 10)
x-intercept	-3.0711	0	(-3.0711, 0)
x-intercept	11.0711	0	(11.0711, 0)
y-intercept	0	6.8	(0, 6.8)
mirror point	8	6.8	(8, 6.8)



12. Use the graph above to find the vertex form for the above arc of a ball through the air.

$$(y - \underline{\hspace{2cm}})^2 = \underline{\hspace{2cm}}(x - \underline{\hspace{2cm}})^2$$

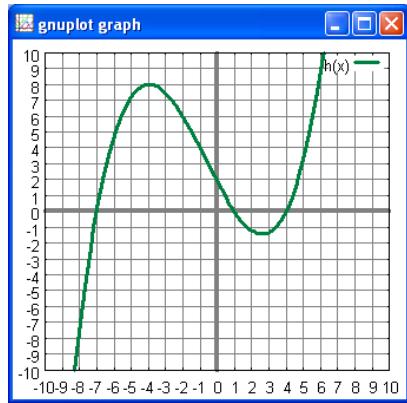
13. Convert the vertex form to quadratic form:  $y = \underline{\hspace{2cm}}x^2 + \underline{\hspace{2cm}}x + \underline{\hspace{2cm}}$

14. [0,       ] Find the y-intercept for  $f(x) = 15x^2 - 34x - 77$

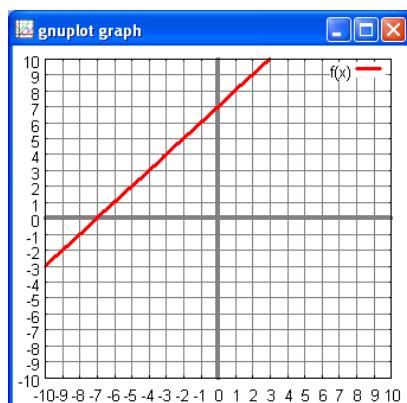
15. Find the zeros of the function  $f(x) = 15x^2 - 34x - 77$  Suggestion: complete the square for  $15x^2 - 34x - 77 = 0$

$$[\underline{\hspace{2cm}}, 0] [\underline{\hspace{2cm}}, 0]$$

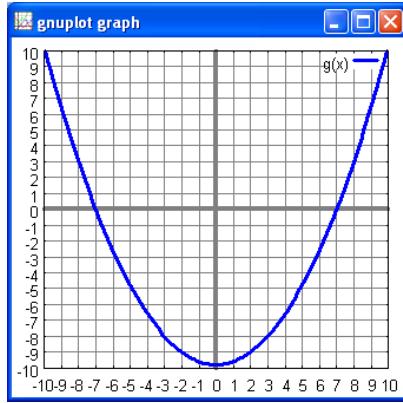
Match the following three graphs below to the correct function below the graphs and name the shape.



A.



B.



C

\_\_\_\_\_ 16.  $f(x) = x + 7$

Name of shape: \_\_\_\_\_

\_\_\_\_\_ 17.  $f(x) = \frac{x^2}{5} - 9.8$

Name of shape: \_\_\_\_\_

\_\_\_\_\_ 18.  $f(x) = \frac{x^3 + 2x^2 - 31x + 28}{15}$

Name of shape: \_\_\_\_\_

19. For the following questions use the three functions:

$$f(x) = 4x - 20$$

$$g(x) = -4x + 20$$

$$h(x) = x^2 + 2x - 143$$

a. \_\_\_\_\_ Find  $(f \circ g)(5)$

b. \_\_\_\_\_ Find  $(g \circ f)(-5)$

c. \_\_\_\_\_ Find  $(f + g)(x)$

d. \_\_\_\_\_ Find  $(f - g)(x)$

e. \_\_\_\_\_ Find  $(f \times g)(x)$

f. \_\_\_\_\_ Find  $(f \div g)(x)$

g. \_\_\_\_\_ Find  $(f \circ g)(x)$

h. \_\_\_\_\_ Find  $(g \circ f)(x)$

i. \_\_\_\_\_ Find the inverse function  $f^{-1}(x)$

j. \_\_\_\_\_ Find the inverse function  $g^{-1}(x)$

k. \_\_\_\_\_ Find  $(f \circ g \circ h)(11)$

20. For the rational function  $r(x) = \frac{(5x^2 - 20)}{(x^2 - 9)}$  determine...

a. The graph of  $r(x)$ . Sketch the graph on the back. You are, of course, free to use the computer based tools of your choice – either Qalculate! or OpenOffice.org.

b. The y-intercept: \_\_\_\_\_

c. The x-intercepts: \_\_\_\_\_ \_\_\_\_\_

d. Determine the domain for  $r(x)$ : \_\_\_\_\_ \_\_\_\_\_

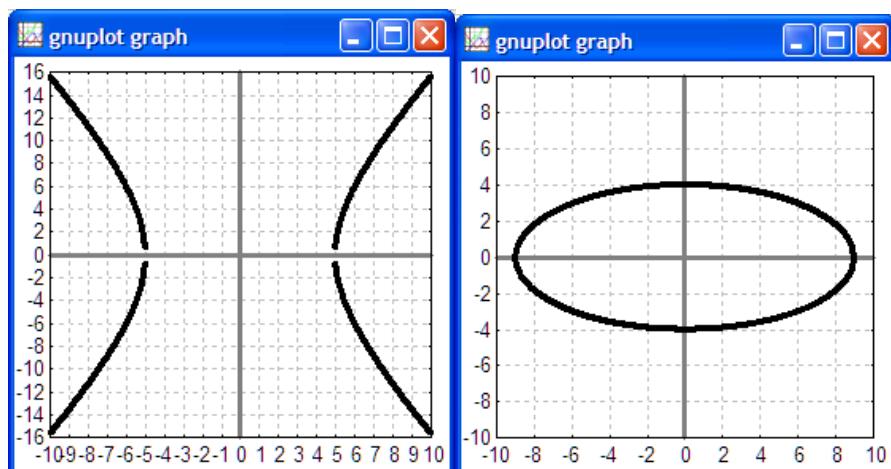
e. The vertical asymptotes: \_\_\_\_\_ \_\_\_\_\_

f. The horizontal asymptote: \_\_\_\_\_

g. Is  $r(x)$  a function? \_\_\_\_\_

h. Is  $r^{-1}(x)$  a function? \_\_\_\_\_

21. Give the name of the following shapes:



22. A wind turbine is used to generate electrical power from the wind. Commercial wind turbines cost about \$1500 per meter of tower height  $h$ . The radius  $r$  of the rotor for a given tower height can be approximated by the function  $r = 0.4h$ . The power  $P$  generated by a wind turbine based on the radius  $r$  and wind velocity  $v$  is given by the function  $P = 1.92 v^3 r^2$

For  $r(h) = 0.4h$  and  
 $P(r) = 1.92 v^3 r^2$

Find  $(P \circ r)(h)$

[http://en.wikipedia.org/wiki/Wind\\_power](http://en.wikipedia.org/wiki/Wind_power)

<http://www.windpower.org/en/tour/econ/index.htm>

<http://www.windpower.org/en/tour/manu/towerm.htm>